## Leadsam Bounds rowarD Math Understanding



## Leapsum Bomnds <br> Toward Math Understanding

## With Leaps and Bounds, mathematics Titerventlon ls as casy as $\mathfrak{1}_{0}$ 2, 38



For more information and full Table of Contents, visit www.nelson.com/leapsandbounds

Kristen sold 305 tickets to the concert. Aki sold 530.


How are 305 and 530 alike?


How are 305 and 530 different?


Choose 305 or 530 . Tell as many things about it as you can Model it in as many ways as you can.


## Representing Numbers to 1000

Pathway 1 GUIDED

A number like 402 might tell how many students are in a school. You can model and show 402 in many ways.

Standard Form

$$
\overbrace{402}
$$

is 4 hundreds +2 ones


- Make a model.

| Hundreds | Tens | Ones |  |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

- Make other models.

$$
402 \text { is also } 3 \text { hundreds }+10 \text { tens }+2 \text { ones. }
$$



402 is also a lot of ones.


You will need

- base ten blocks
- a place value chart


## Remember <br> - 1 ten is 10 ones.

$\rightarrow \rightarrow 00000000$ - 1 hundred is 10 tens.

- You add the hundreds, tens, and ones parts of the number to know the size of the number. e.g., $402=4$ hundreds +2 ones In 402 there are 3 digits: 4,0 , and 2.

2. a) Model 501 using 6 base ten blocks. Sketch your model.

| Hundreds | Tens | Ones |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |

## Write the expanded form:

$$
\ldots \text { hundreds }+_{\ldots} \text { tens }+_{\ldots} \text { ones }
$$

b) Model 150 using 6 base ten blocks. Sketch your model.

| Hundreds | Tens | Ones |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |

## Try These

1. Write each number in standard form.
a) 1 hundred +1 one $=$ $\qquad$
standard form the usual way we write numbers e.g., 231
b) 2 hundreds +2 tens $=$ $\qquad$
$\qquad$
d) 6 hundreds $=$ $\qquad$
2. a) Model another number using 6 base ten blocks.

Sketch your model.


Write the standard form:
Write the expanded form:
b) Model a number greater than 6 using 6 blocks.

Sketch your model.


Write the standard form: $\qquad$
Write the expanded form:
c) Model your number from part b) using 15 blocks.


Write the standard form: $\qquad$
Write the expanded form:
$\qquad$ -

FY
If you can represent numbers in lots of ways, you will
be able to add,
subtract, multiply, and divide. You will also understand
4. Write a number that fits the clue. Model it with base ten blocks in 2 ways. Sketch your models.
a) a little more than one hundred

b) about two hundred

c) more than fifty-one but less than eighty-two

| Sketch: | Sketch: |
| :--- | :--- |
|  |  |

5. Draw a line to match each clue with a number.
a) The tens digit is 0 .
b) The ones digit is the greatest it can be. 203
c) The hundreds digit is greater than 5 .
d) The number has 2 tens.
e) 6 blocks can be used to model the number.
6. Make up a number for each clue.
a) The tens digit is greater than the ones digit or the hundreds digit.
b) 10 blocks are needed to model the number.
c) The hundreds digit is 8 .
d) The ones digit is the least it can be.

## Representing Numbers to 100

42 people are at the pool． 24 people are in the gym．


How are 42 and 24 alike？


How are 42 and 24 different？


Choose 42 or 24 ．Tell as many things about it as you can
Model it in as many ways as you can．


## You will need

－base ten blocks －a place value chart －linking cubes

## Representing Numbers to 100

Pathway 2 GUIDED

A children＇s book by Margaret Mahy is called 17 Kings and 42 Elephants． You can model and show 42 in many ways．

－Make other models．
42 is also 3 tens +12 ones．


42 is also a lot of ones．

| 聞 | 闌 | （4） |  |
| :---: | :---: | :---: | :---: |
| 10 | 10 | 10 | 10 |

## You will need

－base ten blocks
－a place value chart
－linking cubes

## Remember

－ 1 ten is 10 ones． $\rightarrow \rightarrow \infty$ 他
－You add the tens and ones parts of the number to know the size of the number． －Each part is called a digit．In 51 ，the digits are 5 and 1 ．

## Try These

1．Write each number in standard form．
a） 1 ten +1 one $=$ $\qquad$
standard form standard form
the usual way we write numbers e．g．， 31
b） 2 tens $=$ $\qquad$ －
c） 4 tens +5 ones $=$ $\qquad$
d） 5 tens +4 ones $=$ $\qquad$
e） 9 tens +9 ones $=$ $\qquad$Number：Representing Whole Numbers
2. a) Model 71 using 8 base ten blocks. Sketch your model.


Write the expanded form: $\qquad$ tens + $\qquad$ ones

b) Model 26 using 8 base ten blocks. Sketch your model.


Write the expanded form: $\qquad$ tens + $\qquad$ ones
c) Model 80 using 8 base ten blocks. Sketch your model.


Write the expanded form: $\qquad$ tens + $\qquad$ ones
d) Model 44 using base ten blocks. Sketch your model.


Write the expanded form: $\qquad$ tens + $\qquad$ ones
e) Model 44 using 17 base ten blocks. Sketch your model.


Write the expanded form: $\qquad$ tens + $\qquad$ ones
3. a) Use 8 blocks to model a number greater than 8 . Sketch your model.


Write the standard form:

Write the expanded form:
$\qquad$

If you can represent numbers in lots of ways, you will be able to add, subtract, multiply, and divide. You will also understand the also understand
numbers better.
b) Model the number in part a) using 17 blocks or 26 blocks. Sketch your model.


Write the standard form:

Write the expanded form:
4. Model a number that fits the clue. Sketch your model.
a) a little less than nineteen
b) about 10 more than sixteen
Sketch:
5. Draw a line to match each clue with a number.
a) The ones digit is 0 .
b) The number has 2 tens.
c) The ones digit is greater than 6 . 70
d) The number can be modelled with 5 blocks.
6. Make up a number for each clue.
a) The tens digit is 6 .
b) The ones digit is greater than the tens digit. $\qquad$
c) The ones digit is 5 .

## Representing Numbers to 20

12 birds are sitting on one branch of a tree.
18 birds are on another branch.


How are 12 and 18 alike?


How are 12 and 18 different?


Choose 12 or 18 . Tell as many things about it as you can. Model it in as many ways as you can.

| Tell | Model |
| :--- | :--- |
|  |  |
|  |  |

## You will need

## - counters

- 10 -frames


## Representing Numbers to 20

12 students are sitting at picnic tables.


## You will need

- counters
- 10-frames


## Remember

- Fill up a 10 -frame starting at the top left.

- Fill up the first row before you start the second row.

| $\circ$ | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |

- Fill up the second row starting at the left. | $०$ | $\circ$ | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 |  |  |  |  |


## Try These

2. Model each number using counters on 10 -frames.

Write the number of tens and ones in each.

a) 11 |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |
|  |  |  |  |  |

___ tens + $\qquad$ ones
b) 19

___tens + $\qquad$ ones
c) 8


$$
\ldots \text { tens }+
$$

$\qquad$ ones
d) 17

___ tens + $\qquad$ ones
e) 4

_tens + $\qquad$ ones
f) 15

____ tens + ones
g) 7

$\qquad$
$\qquad$ ones

## Remember

 You might not always need to use both 10-frames.3. a) Model a number using one or two 10 -frames. Choose a number you did not use in Question 2.


Write the number of tens and ones.
$\qquad$
$\qquad$ ones
b) Model another number using one or two 10 -frames. Choose a number you have not modelled yet.


Write the number of tens and ones.
$\square$ ones
4. Write 2 numbers to match each clue. Use the numbers 1 to 20.
a) One 10 -frame is a bit more full than the other.
b) Only complete rows are filled with counters.
$\qquad$
$\qquad$
c) Most of one 10 -frame is full.
$\qquad$ -
d) Most of two 10 -frames are full.
$\qquad$
e) One 10 -frame is much more full than the other.
$\qquad$
$\qquad$
f) There are more ones than tens.

## Skip Counting to 1000

## Skip Counting to 1000

You can skip count to figure out the number of cents in groups of coins.


- Skip count forward from 375. Show as many ways as you can.

- Skip count back from 825. Show as many ways as you can.


What do you notice about the digits that change in the numbers? Tell as many things as you can.

You skip count when you are trying to count a group quickly.


You also skip count to put numbers on a number line.


- To skip count forward by 100 s or 10 s, you must put on an extra 100 or an extra 10 each time.
To count forward by 100 s from 462, you could say 462, 562, 662,.
To count forward by 10s from 462, you could say 462, 472, 482, 492...
If you want to add another 10 after 492 ,
you will have 10 tens and can trade them for
1 hundred. The next number is 502 .
4 hundreds +10 tens +2 ones $=5$ hundreds + 0 tens +2 ones
$\overbrace{}^{+10} \overbrace{}^{+10} \overbrace{}^{+10}+{ }^{+10}$
$462,472,482,492,502,512, \ldots$

- Skip counting backward by 100s or 10s works the same way, but you have one fewer 100 or 10 each time.
To count backward by 100s from 633, you could say 633, 533, 433, ...
To count backward by 10s from 633, you could say $633,623,613,603, \ldots$. If you want to remove another 10 after 603, you need to think of one of the hundreds as 10 tens, and take away one of the tens.
6 hundreds +0 tens +3 ones $=5$ hundreds + 10 tens + 3 ones

633, 623, 613, 603, 593, 583, ...


- To skip count forward and backward by 25 , think about quarters and the numbers $25,50,75$, and 100.
To skip count forward by 25s from 325, you would count 325, 350, 375,
400,...
- To skip count backward by 25s, you go in reverse.

$875,850,825,800,775,750, \ldots$


## Try These

1. Count forward to continue each skip counting pattern.


## Remember

When you count by 100s, the tens and ones digits don't change.
When you count by 10s, the ones digit doesn't change.
When you count by 25s, think about quarters.

2. Count backward to continue each skip counting pattern.

3. There is a mistake in these counting by 10 s patterns. Correct the mistake.
a) $378,388,398,3108,3118,3128, \ldots$
b) $723,713,703,793,783,773, \ldots$
4. You skip count from 325 to 525 .

List the numbers you would say in between.
Show as many solutions as you can.
5. Why is skip counting forward or backward by 10 the same as adding or subtracting $10 ?$
$\qquad$
6. Sometimes when you skip count by 10 s, the hundreds digit changes (180, 190, 200, 210).
Sometimes it doesn't (180, 190, 200, 210). When does it change? Why?

## Skip Counting to 100

Pathway 2 OPEN-ENDED

You can skip count to figure out the number of dollars and cents in groups of coins.


- base ten blocks
- 100 chart
- 100 bead chain
- Skip count forward from 35. Show as many ways as you can.

- Skip count down from 85 . Show as many ways as you can.


What do you notice about the digits that change in the numbers? Tell as many things as you can.

## Skip Counting to 100

You skip count when you are trying to count a group quickly.


You also skip count to put numbers on a number line.

| 1 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | 10 | 20 | 30 |  |

- To skip count forward by 10s, you must put on an extra 10 each time.
To count by 10 s, you could say $32,42,52,62 \ldots$
Notice that it is the tens digit that changes.
If the numbers are on a 100 chart, you just go down one row.

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

- To count forward by 5 s or $2 s$ on the 100 chart, you use the grey numbers for 5 s or the striped ones for 2 s .
To count by 5 s , you might count $45,50,55,60,65, \ldots$.
To count by 2 s , you might count $82,84,86,88,90, \ldots$.

|  |  |
| :---: | :---: |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |

Remember

- When you count by 10s, the ones digit does not change. When you count by 5 s , the ones digits flip back and forth between 2 digits.
When you count by 2 s , there is a pattern in the ones digits (2, 4, 6, 8, 0).
- To count backward, you use the same numbers as counting forward, but go the other way.
To count back by 5 s from 75 , you would say $75,70,65,60, \ldots$.


## Try These

1. Count forward to continue each skip counting pattern.



FY
Skip counting is a way to use patterns to add or subtract withou
actually thinking about the addition or subtraction.
2. Count backward to continue each skip counting pattern.

3. There is a mistake in these counting by 5 s patterns.

Correct the mistake.
a) $35,40,45,410,415,420, \ldots$
b) $95,90,85,80,85, \ldots$

## Skip Counting to 20

## Skip Counting to 20

Use 20 counters.


## You will need

- counters
- 10 -frames

Show as many ways as you can to count the counters. Write all the numbers you say for each way you count.


You are "ij" in a game of hide-and-seek. You count down starting at 20. You want to count faster than by 1 s . What might you count by? Write down all the numbers you say.

$\square$
What other ways could you count?


You skip count when you are trying to count a group quickly.


You also skip count to put numbers on a number line.


There are lots of ways to count. Sometimes we start at 1 and sometimes we start at other numbers.
Sometimes we count more than one at a time.

- To count by 2 s , you need to go up by 2 each time.

To count by 2 s starting at 4 , you would say
4, 6, 8, 10, 12, 14, ...
There is a pattern in the ones digits.
This is called skip counting because you skip some of the counting numbers:

$$
4,5,6,7,8,9,10,11,12,13,14, \ldots
$$

- To count forward by 5 s , think of the numbers 5, 10, 15, 20.

| 5 | 10 |  | 15 |  |  |  |  |  | 20 |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\bigcirc \cdot \circ \cdot 0$ | $\cdots \circ \cdot 0$ |  | - 0 | - 0 | - | - |  | - |  | - | - | 。 | - | - | - |  |  |
|  | $\cdots \cdot \circ \cdot 0$ |  | - $\cdot$ | $\bigcirc \cdot$ |  |  |  |  |  | $\bigcirc$ | - | - | - | - | - | - |  |

- To count backward, you use the same numbers as counting forward, but you go the other way.
To count backward by 2 s from 16 , you would say 16, 14, 12, 10, 8, 6, ...


## You will need

- counters
- play coins (pennies
and nickels)
- 10-frames


## Try These

1. Sketch the groups of buttons or use counters. Count them in groups of 2 . Write the numbers you would say.
a) 6 groups of 2 buttons

b) 8 groups of 2 buttons

c) 9 groups of 2 buttons and 1 extra button

2. Continue the skip counting pattern on the number line.

3. Continue the skip counting pattern on the number line.

4. You start at 4 and skip count by 2 s. Write 3 numbers you will not say.

## Comparing and Ordering to 1000

Maya gives these clues about 2 numbers:
Both numbers have the same 3 digits.

- One number is much greater than the other.

What could the 2 numbers be?
List a few possible answers.
$\qquad$
$\qquad$ You will need

- base ten blocks - a place value chart - number lines

Pick one of your sets of numbers.
How do you know which number is greater?

Pick one of your sets of numbers.
How do you know that the greater number is much greater?

## Comparing and Ordering to 1000

Pathway (1) guided

One school has 512 students.
Another school has 378 students.
You can compare the numbers to decide
which school has more students.

- Model the numbers with base ten blocks and compare.


The number with more larger blocks is greater. $512>378$

- Compare both numbers to a nearby number.

512 is more than 500.
378 is less than 500.

- Use a number line.

512 is to the right on the number line.


## Try These

1. Which number is greater, 486 or 417 ?


Both numbers have $\qquad$ hundreds.
$\qquad$ has more tens than $\qquad$ .
$\qquad$ is more than 480 .
$\qquad$ is less than 480.

Which symbol makes the statement true? Circle it. $486><417$
2. Circle the greater number in each pair.
a)

or

$)^{\oplus 日}$
b)

or

c)

or

d)

or

3. Circle the greater number in each pair
a) 513 or 531
b) 881 or 188
c) 113 or 311
d) 372 or 327

FY
Comparing numbers is useful when you have a choice about which of 2 things to buy or get. It also helps you decide if answers make sens when you add and subtract.
e) 66 or $65 \square$
4. Write $>$ or < to compare the 2 numbers. Explain your answer. a) $572 \square 417$
b) $\qquad$

Number: Comparing and Ordering Numbers Leaps and Bounds $3 / 4$ (Draft) Copyright © 2011 by Nelson Education Ltd.
c) $5 \square 1 \square 4 \square 1$
5. List 3 numbers that are greater than the given number.
a) 132 $\qquad$  $\qquad$ --
b) 299 $\qquad$
$\qquad$
$\qquad$
c) 317 $\qquad$
$\qquad$
$\qquad$
d) 972 $\qquad$
$\qquad$
$\qquad$
6. Name a number that is greater than the first number and less than the second number. You can use the number line to help.
a) 678 $\qquad$ 872
b) 412 $\qquad$ 589

d) 612 $\qquad$ 618
7. Use all of the given digits to make 3 different three-digit numbers. Then put the numbers in order.
a) Use 1,3 , and 5 .

Your 3 numbers:
3 numbers in order:
$\qquad$
$\qquad$
$\qquad$
b) Use 1,3 , and 9 .

Your 3 numbers:
3 numbers in order: $\qquad$
$\qquad$
$\qquad$
c) Use 2,5 , and 0 .

Your 3 numbers: $\qquad$
$\qquad$
3 numbers in order: $\qquad$

## Comparing and Ordering to 100

Pathway 2 GUIDED

One student has 51 books.
Another student has 37 books.
You can compare the numbers to decide which student has more books.

- Model the numbers with base ten blocks and compare.


The number with more larger blocks is greater. 5 tens is more than 3 tens.
$51>37$

- Compare both numbers to a nearby number.

51 is more than $50: 37$ is less than 50 .

- Use a number line.


51 is to the right on the number line.
51 is past 50 and 37 is before 50 .

## You will need

- base ten blocks
- a place value chart
- blank number lines


## Remember - Check the tens first to decide which is greater. <br> - Check the ones only if you need to. - More blocks does not mean a bigger number.

## Try These

1. Which number is greater, 48 or 41 ?

Both numbers have $\qquad$ tens.
$\qquad$ has more ones than $\qquad$ .
$\qquad$ is more than 45 .
$\qquad$ is less than 45.
2. Circle the greater number in each pair.


c)
再 ~
or

or

or $\frac{0}{0}$
d)
or
3. Circle the greater number in each pair.
a) 51 or 15

FY
Comparing numbers
is useful when you have a choice about which of 2 things to buy or get. It also buy or get. II also
helps you decide if helps you decide if answers make sense
when you add and
subtract.
e) 6 or 5
4. Write $>$ or $<$ to compare the 2 numbers. Explain your answer.
a) $72 \square 47$
b) 81 or 88
c) 21 or 11
d) 32 or 27
b) $\qquad$ 49
c) $\square$
$\qquad$ 9
$\qquad$
) 5
5. List 3 two-digit numbers that are greater than each number.
a) 34 $\qquad$
$\qquad$
$\qquad$

## Comparing and Ordering to 20

Two numbers are farther apart than 1 and 9. What could the greater number be? List as many answers as you can. Explain your answers.


You will need

- counters
- 10-frames
- number lines

Which number is the greatest? $\qquad$
b) Make 3 more numbers using the cards.

Which number is the greatest? $\qquad$
c) Is it possible to make a greater number? Tell why or why not.

$\qquad$
8. There are more numbers between 51 and 61 than between 47 and 57 . Do you agree or disagree?
Explain your thinking

## Comparing and Ordering to 20

Pathway 3 GUIDED

One group has 11 children. Another group has 9 children You can compare the numbers to decide which group has more.

- Model the numbers and compare.


9 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 |  |

$11>9$

- Compare both numbers to a nearby number. $11>9$ since 11 is more than 10 and 9 is less than 10 .
- Use a number line.

11 is to the right of 9 on a number line.

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## You will need

- counters
- 10-frames
- number lines


## Remember

 - There are different ways to compare numbers.You can use models or counting.

- Line up the number of counters and compare.


## 000000000 <br> 000000000

$11>9$ since there are leftovers.

- Count to see which number you say first.



## Try These

1. Circle the greater number in each pair.
a) $\begin{aligned} & a 0 \\ & 0 \\ & 0\end{aligned}$ a)
00
00
0
or 00
00
00
0
c) $\begin{array}{rl}0 & 0 \\ 0 & 0\end{array}$ 0
0
0
0
b) $\begin{array}{lll}0 & 0 & 0 \\ 0 & 0 & 0\end{array}$ 0 or 00000 -
d) 1 00
00
00
or
2. Circle the greater number in each pair.
a) 12 or 8
b) 15 or 17
c) 9 or 2
d) 10 or 12
e) 7 or 15
f) 17 or 9
g) 20 or 13
h) 1 or 8
3. Name a number that is a little bit less than each number.
a) 14 $\qquad$ c) 15 $\qquad$
b) 10 $\qquad$ d) 8 $\qquad$
4. Name a number that is a little bit more than each number.
a) 18 $\qquad$ c) 12 $\qquad$
b) 10 $\qquad$ d) 3 $\qquad$
5. a) Make 2 numbers using 2 cards at a time.

Which number is greater? $\qquad$
b) Make 3 more numbers using the cards.
$\qquad$ - $\qquad$ - $\qquad$ -

Which number is the greatest? $\qquad$
6. Name a number that is greater than the first number and less than the second number. Use the number line below.
a) 3 $\qquad$ 8
c) 9 $\qquad$ 16
b) 14 $\qquad$ 18
d) 15 $\qquad$ 18

7. There are more numbers between 0 and 10 than between 10 and 20. Do you agree or disagree? Explain your thinking.

## Leepsam Boundr rownio math Ondersiandity

## With Leaps and Bounds, mathematics Thervention ls es easy as $\eta_{0}$ 2 38



Grades 3-4

Leaps mom Bounds TOWARD Math Understanding

Leaps mo Bounds roward Math Understanding

Visit www.nelson.com/leapsandbounds for more information.
Grades 7-8
Grades 5-6

