2. b)

c)

d)

e)

3. The three prisms can have dimensions 2 cm $\times 9 \mathrm{~cm} \times 10 \mathrm{~cm} ; 3 \mathrm{~cm} \times 6 \mathrm{~cm} \times 10 \mathrm{~cm} ; 6 \mathrm{~cm}$ $\times 6 \mathrm{~cm} \times 5 \mathrm{~cm}$; or any other combination of three numbers that multiply to give $180 \mathrm{~cm}^{3}$.
4. 

| Length <br> (cm) | Width <br> (cm) | Height <br> (cm) | Surface <br> Area (cm |
| :---: | :---: | :---: | :---: |
| 100.0 | 40.0 | 50.0 | 22000 |
| 90.0 | 44.4 | 50.0 | 21432 |
| 80.0 | 50.0 | 50.0 | 21000 |
| 70.0 | 57.1 | 50.0 | 20704 |
| 60.0 | 66.7 | 50.0 | 20674 |
| 50.0 | 80.0 | 50.0 | 21000 |

According to the chart above, a base with length $=60.0 \mathrm{~cm}$ and width $=66.7 \mathrm{~cm}$ results in the smallest surface area. This is a good answer. However, you can keep going to find a better answer. Notice that these dimensions are almost equal. From this, you can guess that a length and width that are equal will result in the smallest possible surface area:

| Length <br> (cm) | Width <br> (cm) | Height <br> (cm) | Surface <br> Area $\left(\mathbf{c m}^{2}\right)$ |
| :---: | :---: | :---: | :---: |
| 63.2 | 63.2 | 50 | 20628.5 |

5. $25 \mathrm{~cm}, 30 \mathrm{~cm}$, and 10 cm

### 11.4 Relating the Dimensions of a Rectangular Prism to Its Volume

1. a) i) $4 \mathrm{~cm} \times 6 \mathrm{~cm} \times 10 \mathrm{~cm}$
ii) $4 \mathrm{~cm} \times 5 \mathrm{~cm} \times 12 \mathrm{~cm}$
b) If you doubled the height of the dimensions in part (i), the new volume would be $480 \mathrm{~cm}^{3}$, or double the original volume.
c) Yes, the new volume would be equal. Doubling any one dimension results in a volume that is doubled.
d) i) $480 \mathrm{~cm}^{3}$
ii) $480 \mathrm{~cm}^{3}$
2. a) $720 \mathrm{~cm}^{3}$
$\begin{array}{ll}\text { b) } 180 \mathrm{~cm}^{3} & \text { c) } 1080 \mathrm{~cm}^{3} \\ \text { d) } 5 \mathrm{~cm} & \text { e) } 100 \mathrm{~cm}\end{array}$ f) 1 cm

### 11.5 Exploring the Surface Area and Volume of Prisms

1. a) $96 \mathrm{~cm}^{2}$ and $64 \mathrm{~cm}^{3}$
b) $136 \mathrm{~cm}^{2}$ and $64 \mathrm{~cm}^{3}$
c) $160 \mathrm{~cm}^{2}$ and $64 \mathrm{~cm}^{3}$
2. a) $64.0 \mathrm{~cm}^{2}$ and $28.0 \mathrm{~cm}^{3}$
b) $64.0 \mathrm{~cm}^{2}$ and $32.0 \mathrm{~cm}^{3}$
c) $64.0 \mathrm{~cm}^{2}$ and $34.848 \mathrm{~cm}^{3}$
3. The prism on the right side has the greatest surface area. If two prisms have the same volume, the prism that is closest in shape to a cube will have the smallest surface area.
4. The prism on the left side has the greatest volume. If two prisms have the same surface area, the prism that is closest in shape to a cube will have the greatest volume.

## Test Yourself

1. a) 78 units $^{2}$
b) 32 units $^{2}$
c) $142 \mathrm{~cm}^{2}$
2. a) 24 units $^{3}$
b) 48 units $^{3}$
c) $360 \mathrm{~cm}^{3}$
3. a) $248 \mathrm{~cm}^{2}$
b) $240 \mathrm{~cm}^{3}$
c) $120 \mathrm{~cm}^{3}$
d) $480 \mathrm{~cm}^{3}$
4. a) $30 \mathrm{~cm}^{3}$
b) 1 cm
c) 3 cm
d) $125 \mathrm{~cm}^{3}$
e) $21 \mathrm{~cm}^{3}$
5. Sandra's tower should be 3 blocks high.

## Chapter 12

### 12.1 Exploring Probability

1. a) probably $\frac{1}{2}$ to 1 , depending on your habits
b) $\frac{1}{2}$
c) 0
d) probably about $\frac{1}{8}$
e) $\frac{1}{2}$
2. a) This is not a fair game.
b) Omar is most likely to win.
3. a) red marble, red marble, blue, blue, blue, yellow, yellow, green, green, green, green green
b) $\frac{3}{12}$ or $\frac{1}{4}$

### 12.2 Calculating Probability

1. a) $\frac{1}{3}$
b) $\frac{1}{3}$
2. a) red + green, red + blue, green + red, green + blue, blue + red, blue + green b) 0.333
3. $\frac{6}{30}$, or $\frac{1}{5}$
4. a) $\frac{1}{4}$
b) $\frac{3}{4}$

### 12.3 Solve Problems Using Organized Lists

1. a)

| \$5 <br> bills | 3 | 2 | 2 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\$ 10$ <br> bills | 0 | 1 | 0 | 2 | 0 | 1 | 3 | 0 | 2 | 1 |
| $\$ 20$ <br> bills | 0 | 0 | 1 | 0 | 2 | 1 | 0 | 3 | 1 | 2 |
| Sum | $\$ 15$ | $\$ 20$ | $\$ 30$ | $\$ 25$ | $\$ 45$ | $\$ 35$ | $\$ 30$ | $\$ 60$ | $\$ 40$ | $\$ 50$ |

b) 10 different combinations are possible
c) 1 combination adds up to $\$ 60$
d) $\frac{1}{10}$
e) $\frac{7}{10}$
2. a)

| Win | 4 | 3 | 3 | 2 | 2 | 2 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Lose | 0 | 1 | 0 | 2 | 0 | 1 | 3 | 0 | 2 | 1 | 4 | 0 | 3 | 1 | 2 |
| Te | 0 | 0 | 1 | 0 | 2 | 1 | 0 | 3 | 1 | 2 | 0 | 4 | 1 | 3 | 2 |

## b) $\frac{1}{15}$

### 12.4 Using Tree Diagrams to Calculate Probability

 b) $\frac{3}{9}$ or $\frac{1}{3}$ c) $\frac{1}{9}$
2. a)

1st child 2nd child 3rd child 4th child 5th child Outcome

b) $\frac{5}{32}$
c) $\frac{10}{32}$, or $\frac{5}{16}$

### 12.5 Applying Probabilities

1. Romona is the most likely to make her next shot.
2. a) Indira is the most likely to win.
b) Bonnie and Simon have the same probability of winning.
3. a) $\frac{1}{4}$
b) $\frac{1}{6}$
c) Paul is the most likely to win.
4. $\frac{1}{3}$
5. a) $B a g B$
b) $\frac{12}{17}$
6. James's throw of 2 was the least likely event.
7. The most likely total is 7 , because you can get it in the most number of ways ( $1+6$, $3+4$, and $2+5$ ).
8. It is not certain that she has touched a Norway maple, although it is very likely. Calculating the probabilities will show that there is a chance of touching three trees in a row that are not Norway maples.

## Test Yourself

1. a) $\frac{2}{3}$
b) $\frac{1}{2}$
2. a) $\frac{3}{10}$
b) $\frac{2}{10}$
c) $\frac{1}{10}$
d) $\frac{2}{5}$
3. a)

| Quarters | 4 | 3 | 3 | 2 | 2 | 2 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Dimes | 0 | 1 | 0 | 2 | 0 | 1 | 3 | 0 | 2 | 1 | 4 | 0 | 3 | 1 | 2 |
| Nickels | 0 | 0 | 1 | 0 | 2 | 1 | 0 | 3 | 1 | 2 | 0 | 4 | 1 | 3 | 2 |
| Total <br> value | 100 | 85 | 80 | 70 | 60 | 65 | 55 | 40 | 50 | 45 | 40 | 20 | 35 | 25 | 30 |

b) $\frac{1}{15}$
c) You are certain to guess them, so the probability is 1 , or $100 \%$.
4. a)

| Story <br> $\mathbf{1}$ | 1 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 3 | 3 | 3 | 4 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Story <br> $\mathbf{2}$ | 1 | 5 | 2 | 4 | 3 | 1 | 4 | 2 | 3 | 1 | 3 | 2 | 1 | 2 | 1 |
| Story <br> $\mathbf{3}$ | 5 | 1 | 4 | 2 | 3 | 4 | 1 | 3 | 2 | 3 | 1 | 2 | 2 | 1 | 1 |

b) $\frac{1}{5}$
c) $\frac{2}{5}$
5. a)

$\begin{array}{ll}\text { b) } \frac{1}{16} & \text { c) } \frac{3}{8}\end{array}$
6.

7. a) Team 2 is the most likely to win.
b) Team 1 is the most likely to lose.
8. a) Romona should choose Tynessa's wallet.
b) $\frac{6}{25}$

