Ontario Numeracy Assessment Package



MEASUREMENT

The Measurement Strand of the Ontario Curriculum for Grade 4 identifies seven Mathematical Process Expectations: problem solving, reasoning and proving, reflecting, selecting tools and computational strategies, connecting, representing, and communicating. Using these process expectations, students study, learn, and apply concepts and skills organized under the big ideas/headings of Attributes, Units, and Measurement Sense, and Measurement Relationships.

The following chart highlights key knowledge and skill development as students move from Grade 4 to 5.

GF	RADE 4		GRADE 5
 estimate, measumeasurements, estimate, measumeasumeasumeasumeasumeasumeasumeasu	ure, and record linear using standard units ure, and record perimeter ygons	•	select and justify the most appropriate standard unit for linear measurements estimate, measure, and record perimeter and area of regular and irregular polygons
 estimate, measu (kilograms, grar millilitres), and taken up by an 	ure, and record the mass ns), capacity (litres, volume (related to space object)	•	select and justify the most appropriate standard unit to measure mass (grams, kilograms, tonnes)
 estimate, measuintervals (neare and determine) 	ure, and represent time st minute) and estimate elapsed time	•	estimate, measure, and represent time intervals (nearest second) and estimate and determine elapsed time
 describe, throug relationship am length, mass, ar 	th investigation, the ong various units of nd capacity	•	solve problems requiring conversion from metres to centimetres and kilometres to metres
 pose and solve that require the perimeter and a 	meaningful problems ability to distinguish Irea	•	solve problems requiring the estimation and calculation of perimeters and areas of rectangles
 determine, thro relationship bet 	ugh investigation, the ween the side lengths of	•	generalize to develop the formula for perimeter, area, and volume
a rectangle and	its perimeter and area	•	create two-dimensional shapes with the same perimeter or the same area
		•	determine, through investigation, the relationship between capacity and volume
solve problems relationship bet and centuries	involving the ween years, decades,	•	solve problems involving the relationship between a 12-hour clock and a 24-hour clock

For each strand of the curriculum, ONAP provides three types of assessment materials. Consider the following points when administering the assessments for the strand:

Part A: Activating Prior Knowledge (page 85)

- The activities in Part A have been created to activate students' prior knowledge before they complete the Part B assessment or the Part C performance tasks.
- No score is assigned during this part of the assessment.
- It is recommended that you spend one or two periods working on and discussing the activities provided in this part.

Part B: Concepts and Skills Assessment (page 90)

- The paper-and-pencil assessment in Part B addresses each of the specific expectations within the two overall expectations in the Measurement Strand.
- Students will be responding to a mix of questions: short-response, fill-in-the-blank, and multiple-choice.
- Most students will be able to complete the entire assessment in a 60-minute period. If necessary, provide students with additional time to complete the assessment, as long as they complete it in one sitting.

Part C: Performance-Based Assessment (page 108)

- The two performance tasks in Part C are designed to provide you with insights into how well students are able to perform measured against the categories of the Ontario Achievement Chart: Knowledge and Understanding, Thinking, Communication, and Application.
- All of the overall expectations for this strand have been assessed through the Concepts and Skills Assessment in Part B.
- It is recommended that you select one performance task for the Measurement Strand.
- Each task is designed to be completed in a 45- to 60-minute period. If necessary, provide additional time as long as students complete the task in one sitting. *Note: Time permitting, students may complete both performance tasks to provide you with additional insight regarding their ability to problem solve, apply mathematical understanding, and communicate effectively.*

Part A: Activating Prior Knowledge

Administration

To activate students' prior knowledge of the Measurement Strand, choose one or two of the following activities to work on prior to administering the assessments. Introductory and culminating suggestions have been provided for each. No score is assigned for these activities.

Timing

It is recommended that you spend one or two periods working on and discussing the activities provided in this part.

Accommodating Students with Special Needs

Observe students as they complete the activities. While the activities in this section are not designed as a formal diagnostic assessment, you may want to consider whether students who are having extreme difficulties with the activities are ready to participate in the full ONAP assessment for this grade level. Observations at this stage might also indicate students who will need special accommodations during the assessment such as someone to read questions to them or to scribe responses.

Activity 1: Measuring Scavenger Hunt

Materials

- BLM A1: Activity 1: Measuring Scavenger Hunt
- metric rulers
- metre sticks or measuring tapes
- tool to measure mass (scale and gram weights)
- calibrated measuring cups in millilitres and litres
- empty plastic containers
- water

Introducing the Activity

Brainstorm with students all the considerations that need to be made before an item is measured (e.g., the units and measuring tool to be used, the precision needed, the method to be used for recording the measurement). List students' suggestions on the chalkboard.

Have students work in pairs to complete the BLM A1: *Activity 1: Measuring Scavenger Hunt.* Make sure that there are enough materials for half of the student pairs to be working on a type of measuring at a time; for example, half of the students measure time and length, while the other half measure mass and capacity.

Culminating Discussion

1. What did you do if your measurement included a part of a unit (for example, a measurement that is longer than 3 m but not as long as 4 m)? Sometimes I just estimated the extra part. I said 3 and $\frac{1}{2}$ m. Sometimes I measured the extra part with smaller units. Then I could say 3 m and 45 cm. This is probably the best way.

- 2. How did you use your measurement of the height of the door to help you estimate the measurement of an object half as high as the door? *I sort of know how high a door is, so when I looked around, I could find things that were about half as high as the door. I know about how far the top of the door is to the ceiling, and I also know about how much taller the door is than I am. This all helped me find something half as high as the door.*
- 3. What is the difference between using a measuring tool to determine a precise measurement and making an estimate? Why might you need to do both? *When I measured with the metre stick, I could see how many centimetres high the chair was. I could have estimated because the chair is not as high as half the door, so I know it is less than 100 cm. Sometimes you need to measure, like when the doctor measures how tall I am, but sometimes an estimate is okay, like when my mom buys me a shirt, and she says this looks like it's about your size.*

Activity 2: Geoboard Challenge

Materials

- geoboards and geobands (preferably 11×11 units; one per student pair)
- BLM A2: Activity 2: Geoboard Challenge (one per student)
- dot paper (one per student)

Introducing the Activity

Use an overhead geoboard to look at a 4 unit by 5 unit rectangle. Discuss how to determine the perimeter (18 units) and area (20 square units) and the units for each measurement. Do the same for a polygon that is not rectangular but follows the geoboard pegs. Discuss the meaning of the term *polygon*. You may also choose to model how to record geoboard figures on dot paper. Have the students work in pairs to complete the activities on BLM A2: *Activity 2: Geoboard Challenge*.

Culminating Discussion

- What did you notice about rectangles that have the same area but different perimeters? *They all have the same number of squares, but they are different shapes.*
- 2. What did you notice about rectangles that have the same perimeter but different areas? *They have different numbers of squares. They start long and skinny and then get more like a big square. The square shapes have the most number of inside squares.*
- 3. How many different rectangles with an area of 48 square units can you draw using whole number units? How would you know if you had found all the rectangles that have an area of 48 square units? You can draw five different rectangles with an area of 48 units: 48 × 1, 24 × 2, 16 × 3, 12 × 4, 8 × 6. To find all the rectangles, I figured out all of the numbers that multiplied to 48. I used an organized list to make sure I found all of them. I started with 1 × 48, then 2 × 24, then 3 × 16. I had to skip some numbers because they did not work, and I stopped when the numbers started to repeat.

Name:	C	Date:
Activity 1: Measur	ing Scavenger Hur	nt
Time		
Write the time that you and y	your partner(s) started the hu	nt:
Write the time that you and y	your partner(s) finished the h	unt:
How much time did you sper Write this time to the nearest	d on the hunt? five minutes:	
Length, Perimeter, and A	rea	
Measure each of the following	5.	
height of a door	measurement:	unit:
length of a pencil	measurement:	unit:
width of the classroom	measurement:	unit:
height of a chair	measurement:	unit:
perimeter of the classroom	measurement:	unit:
area of a desktop	measurement:	unit:
Find one object in the room to Measure the object. Was your	hat is about half as high as the stimate reasonable?	he door.
name of object:	height of object:	unit:
Mass		
What is the mass of 20 patter	n block hexagons (yellow blo	ocks)?
estimate:	measurement:	unit:
What is the mass of your mat	h textbook?	
estimate:	measurement:	unit:
Capacity		
Use the measuring cups and v	vater to determine the capaci	ty of the three containers.
Container 1	measurement:	unit:
Container 2	measurement:	unit:
Container 3	measurement:	unit:

Name:

Date: _____

Activity 2: Geoboard Challenge (page 1)

Challenge 1

Create as many different rectangles as you can that have a perimeter of 24 units.

. • • .

Create three different polygons that are not rectangles but also have a perimeter of 24 units.

•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•
•	•	·	•	•	·	·	•	•	•	•	•	•	•	•	•	•	•	•	•	•
•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•
	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•
													•			•				

Challenge 2

Create as many different rectangles as you can that have an area of 18 square units.

•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•
•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	
•		•	•	•	•	•	•	•	•	•		•							•	

Create three different polygons that are not rectangles but also have areas of 18 square units.

. .

Name: _____ Date: _____

Activity 2: Geoboard Challenge (page 2)

Challenge 3

Create two rectangles that have the same area but different perimeters.

•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•
•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•
				•				•											•	
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Create a rectangle that has an area of 20 square units and a perimeter of 24 units.

•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•
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•	•	•		•	•		•	•		•	•	•	•	•	•	•	•			•
•	•	•	•	•	•	•	•	•	•	•	•	•	•	·	•	•	•	•	•	•
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•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•

Create two different polygons that are not rectangles. Each polygon should have an area of 12 square units.

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	•								•		•	•	•	•		•				•
.														•						

Part B: Concepts and Skills Assessment

Administration

The paper-and-pencil assessment in Part B addresses each of the specific expectations within both of the overall expectations in the Measurement Strand. Part B includes several styles of questions: short-response, matching, fill-in-the-blank, and multiple-choice.

Timing

Most students will be able to complete the entire assessment in a 60-minute period. If necessary, provide students with additional time to complete the assessment as long as they complete it in one sitting.

Materials

	FOR THE TEACHER		FOR EACH STUDENT		FOR EACH GROUP OF STUDENTS
•	Individual Student Scoring Guide: p. 100	•	Assessment Part B: p. 92	•	colour tiles connecting cubes
•	Class Tracking Sheet: p. 104 ONAP 5 CD-ROM (optional)	• • •	pencil eraser ruler centimetre grid paper		

Introducing the Assessment

Inform students that they will be completing an assessment to help you get to know what they have learned about math in earlier grades. Tell students that it is important that they answer the questions as fully as possible. To communicate effectively, they can use pictures, numbers, words, and/or diagrams to represent their thinking.

Point out the manipulative materials you have provided for students to use throughout the assessment. Encourage students to access other materials available in the classroom that they think might help them to answer questions and/or solve problems.

Note: Calculators are not recommended during this assessment.

Accommodating Students with Special Needs

If individuals or groups of students have difficulties with reading, consider reading the questions orally as they complete the assessment.

If individual students have difficulties explaining their thinking in writing, consider providing scribes to record for the students or encourage students to show and explain their thinking using concrete materials.

Some students will require additional time to complete the assessment. You may wish to note this accommodation in your anecdotal records about the student. However, there should be no reduction of the student's overall score in terms of the amount of time it takes the student to complete the assessment.

Scoring the Assessment

A detailed Individual Student Scoring Guide has been provided on page 100. The guide is designed to be completed for each student. The individual scores can then be used to fill in the Class Tracking Sheet. Alternatively, you may record student results directly on the Class Tracking Sheet. The results can be recorded on a photocopy, or electronically using the ONAP 5 CD-ROM.

While great care has been taken to consider the range of possible answers for each question, there will be times when you will need to apply your professional judgment to score an individual answer. You may use the Curriculum Correlation chart provided on page 106 to help you to determine whether the student has demonstrated the intended concept knowledge or skill based on the overall and specific expectations being assessed by the particular question.

At times a student may provide an answer that you think does not completely represent his or her knowledge and skill level. You may ask probing questions to better assess the student's overall understanding.

Some questions are delivered in more than one part (a and b) and are given more than one point. Should a student's answer in one part reveal that a correct answer in the other part was arrived at for the wrong reason, a score of zero should be given for both parts.

Summarizing Individual and Class Achievement

Once you have completed scoring the students' assessments, you will need to record the results. You may record the results electronically using the ONAP 5 CD-ROM, or use a photocopy of the Class Tracking Sheet provided on pages 104 and 105.

Name:

Date: _

Measurement

1. What is the length of the line segment in millimetres?

2. Use a ruler to draw a line segment that is 95 mm long.

3. Write the time.



- 4. You leave school at 3:30 p.m. It takes you
 - 20 minutes to walk to your friend's house,
 - then 10 minutes to eat a snack,
 - then 25 minutes to play a video game,
 - then 10 minutes to walk home, and
 - then 30 minutes to do your homework.

At what time will you be finished your homework?

- **A** 5:00 p.m. **C** 5:05 p.m.
- **B** 6:00 p.m. **D** 6:05 p.m.

ONAP

Nai	me:	Date:	
5.	Use the centimetre grid to measure perimeter and the area of each poly	the gon.	
	a) perimeter:		
	area:		
	b) perimeter:		
	area:		
6.	Estimate the mass of three math tex Circle the answer you think is most	tbooks. reasonable.	
	A 15 g		MATHEMATICS 5
	B 3 kg		MATHEMATICS 5

- **C** 300 g
- D 750 g



volume of the prism: _____

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ONAP



Name:	Date:
b)	the distance between two cities:
	Explain your thinking.
11 . Th	e area of a rectangle is 20 cm ² . The length of one side is 5 cm.
	5 cm
	cm
۵)	What is the length of the other side?
b)	What is the perimeter?
12. a)	Can two rectangles have the same area but different perimeters?
	YES NO
	Explain your thinking.
b)	Circle either area or perimeter to complete the following sentences.
	I need to know about <i>area</i> / <i>perimeter</i> if I want to seed the schoolyard with new grass.
	I need to know about <i>area / perimeter</i> if I want to build a

Nai	me: Date:
13.	Order these four amounts from least capacity to greatest capacity: 3 L, 3004 mL, 2.2 L, 2950 mL
14.	How many of each of the weights shown (labelled A, B, C, D, and E) do you need to balance this scale? Write the number needed of each weight beside the letter label in the table below.
	1 kg 500 g 250 g 100 g 10 g
	A B C D E
15.	This container of fruit juice was full to the 1 L mark before Greg had a drink. How many millilitres of fruit juice did Greg drink?

250 mL –

number of millilitres Greg drank: _____

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Nam	e:	Date:
16. d	a)	What is the most appropriate unit of mass to measure each of the following (milligrams, grams, kilograms)?
		a calculator:
		a desk:
		Explain your thinking.
ł	b)	What is an appropriate unit of mass to measure each of the following (millilitres, litres)?
		a glass of water:
		a bag or carton of milk:
		Explain your thinking.
47		
17. 0	a)	Canada became a country in 1867. Canada has been a country for
		A more than two centuries
		 Less than two conturies
		\mathbf{D} exactly two centuries
ł	b)	A grandmother is 87 years old. How many complete decades has she lived?
		A eight
		B nine
		C seven
		D ten

Name	:												Da	te: _		
18. a)	Dra 12 u	w th inits	ree o , on	diffe the	rent grid	rect pap	ang ber. l	les, e Labe	each l the	wit e len	h a igth	perii s of	mete the	er of sides		

b) Draw three different rectangles, each with an area of 36 square units, on the grid paper. Label the lengths of the sides.

ONAP INDIVIDUAL STUDENT SCORING GUIDE GRADE 5: MEASUREMENT - PART B

Name:	Date:								
Overall Expectation 4m38 (Attributes, Units, and Measurement Sense): Estimate, measure, and record length, perimeter, area, mass, capacity, volume, and elapsed time, using a variety of strategies.									
4m40 1	65 mm or 6 cm and 5 mm (accept any answer between 63 mm and 67 mm) 1 point								
4m41 2	1 point for drawing a line that measures 95 mm long (accept any answer between 93 mm and 97 mm)								
4m42 3	 2:27 or two twenty-seven or twenty-seven after two; 11:40 or eleven forty or 20 minutes before (or of) 12 1 point for both correct answers 								
4m43 4	C 1 point								
4m44 5 a)	Perimeter: 18 cm Area: 12 cm ² 1 point for two correct dimensions								
4m44 5 b)	Perimeter: 14 cm Area: 8 cm ² 1 point for two correct dimensions								
4m45 6	B 1 point								
4m46 7 a)	2 L or 2000 mL 1 point								
4m46 7 b)	7 1 point								

4m47		
8	60 cubes	
	1 point	
	Total for Overall Expectation 4m38	
		10
Overall	Expectation 4m39 (Measurement Relationships):	
Determ perime	ine the relationships among units and measurable attributes, including the area and ter of rectangles.	
4m48		
9 a)	A	
	1 point	
4m48		
9 b)	с	
	1 point	
4m49		
10 a)	1 point for a partial explanation that demonstrates some understanding, e.g., <i>Metres are</i>	
	too big.	
	OR 2 points for a complete explanation that demonstrates full understanding, e.g., <i>Metres and</i> kilometres are way too big. It could be millimetres, but the number would be big so I'd use	
	centimetres.	
4m40		
10 b)	1 point for answering "kilometres" and a partial explanation that demonstrates some	
	understanding, e.g., I've seen signs on the road that show kilometres.	
	OR 2 points for answering "kilometres" and a complete explanation that demonstrates full	
	like kilometres, makes sense.	
4m50		
iia)	4 cm	
	, bour	
4m50		
11 b)	18 cm	
	1 point	
4m51		
12 a)	1 point for answering "Yes" and a partial explanation that demonstrates some understanding,	
	e.g., You can spread out the space in different ways.	
	UK 2 points for answering "res" and and a complete explanation that demonstrates full understanding, e.g., <i>Two rectanales can have an area of 20 but have different perimeters:</i>	
	4×5 and 10×2 .	

4m51 12 b)	area; perimeter 1 point for two correct responses	
4m52 13	2.2 L, 2950 mL, 3 L, 3004 mL 1 point	
4m53 14	Sample answer: 5 A, 1 C 5 A, 2 D, 5 E 4 A, 2 B, 1 C or any other combination of weights that adds to 5250 g 1 point	
4m54 15	250 mL 1 point	
4m55 16 a)	1 point for answering "grams" and "kilograms" and a partial explanation that demonstrates some understanding, e.g., <i>A calculator is smaller, so grams for calculators and kilograms for a desk.</i> OR 2 points for answering "grams" and "kilograms" and a complete explanation that demonstrates full understanding, e.g., <i>A kilogram weighs about the same as a book. A calculator is much lighter than a book and a desk is much heavier. Since grams are light, I'd use them for the calculator and kilograms for the desk.</i>	
4m55 16 b)	1 point for answering "millilitres" and "litres" and a partial explanation that demonstrates some understanding, e.g., <i>We buy bags or cartons of milk marked litres. Glasses hold less.</i> OR 2 points for answering "millilitres" and "litres" and a complete explanation that demonstrates full understanding, e.g., <i>A litre is 1000 mL. A litre is like a container of ice cream, so that's about the same size as a small bag or carton of milk. It could even be more. A glass of water holds a lot less, so I'd use a smaller unit like millilitres.</i>	
4m56 17 a)	C 1 point	
4m56 17 b)	A 1 point	

4m57		
18 a)	1 point for drawing two correct rectangles with two adjacent sides adding up to 6, e.g., 3×3 , 4×2 , or 5×1	
	OR 2 points for drawing all three rectangles with two adjacent sides adding up to 6, e.g., 3×3 , 4×2 , 5×1	
	NOTE: Credit should be given to students who correctly identify a decimal or fraction (mixed number) solutions.	
4m57		
18 b)	1 point for drawing and labelling two rectangles with two adjacent sides that, when multiplied, equal 36	
	OR 2 points for drawing and labelling three rectangles correctly: i.e., three of, for example, 36×1 , 18×2 , 12×3 , 9×4 , 6×6	
	NOTE: Credit should be given to students who correctly identify decimal or fraction (mixed number) solutions.	
	Total for Overall Expectation 4m39	24

Date:		(Grade:			Schoo	l:						
Overall Expe		4m38 (Attributes, Units, and Measurement Sense) Estimate, measure, and record length, perimeter, area, mass, capacity, volume, and elapsed time, using a variety of strategies											
Spe	ecific Expe	tation #	4m40	4m41	4m42	4m43	4m	144	4m45	4n	146	4m47	_
-1-	Q	uestion #	1	2	3	4	5(a)	5(b)	6	7(a)	7(b)	8	Tota
Student Name	Gender (M/F)	IEP/ELL											

CLASS TRACKING SHEET – PART B

Board: _____ Teacher Name: _____

	4m39 (Measurement Relationships) Determine the relationships among units and measurable attributes, including the area and perimeter of rectangles.																
4r	n48	4m	າ49	4n	n50	4n	n51	4m52	4m53	4m54	4n	n55	4r	n56	4r	n57	_
9(a)	9(b)	10(a)	10(b)	11(a)	11(b)	12(a)	12(b)	13	14	15	16(a)	16(b)	17(a)	17(b)	18(a)	18(b)	Tota

ONTARIO CURRICULUM CORRELATION TO ONAP MEASUREMENT 5 - PART B

NOTE: This correlation is to the Grade 4 Ontario Curriculum Expectations.

Overall Expectation 4m38 (Attributes, Units, and Measurement Sense):

Estimate, measure, and record length, perimeter, area, mass, capacity, volume, and elapsed time, using a variety of strategies.

Question Number	Specific Expectation
1	4m40: estimate, measure, and record length, height, and distance, using standard units (i.e., millimetre, centimetre, metre, kilometre) (e.g., a pencil that is 75 mm long)
2	4m41: draw items using a ruler, given specific lengths in millimetres or centimetres
3	4m42: estimate, measure (i.e., using an analogue clock), and represent time intervals to the nearest minute
4	4m43: estimate and determine elapsed time, with and without using a timeline, given the durations of events expressed in five-minute intervals, hours, days, weeks, months, or years
5 a)-b)	4m44: estimate, measure using a variety of tools (e.g., centimetre grid paper, geoboard) and strategies, and record the perimeter and area of polygons
6	4m45: estimate, measure, and record the mass of objects (e.g., apple, baseball, book), using the standard units of the kilogram and the gram
7 a)-b)	4m46: estimate, measure, and record the capacity of containers (e.g., a drinking glass, a juice box), using the standard units of the litre and the millilitre
8	4m47: estimate, measure using concrete materials, and record volume, and relate volume to the space taken up by an object (e.g., use centimetre cubes to demonstrate how much space a rectangular prism takes up)
Overall Expectat Determine the r of rectangles.	tion 4m39 (Measurement Relationships): elationships among units and measurable attributes, including the area and perimeter
9 a)–b)	4m48: describe, through investigation, the relationship between various units of length (i.e., millimetre, centimetre, decimetre, metre, kilometre)
10 a)–b)	4m49: select and justify the most appropriate standard unit (i.e., millimetre, centimetre, decimetre, metre, kilometre) to measure the side lengths and perimeters of various polygons
11 a)-b)	4m50: determine, through investigation, the relationship between the side lengths of a rectangle and its perimeter and area

Question Number	Specific Expectation
12 a)-b)	4m51: pose and solve meaningful problems that require the ability to distinguish perimeter and area (e.g., "I need to know about area when I cover a bulletin board with construction paper. I need to know about perimeter when I make the border.")
13	4m52: compare and order a collection of objects, using standard units of mass (i.e., gram, kilogram) and/or capacity (i.e., millilitre, litre)
14	4m53: determine, through investigation, the relationship between grams and kilograms
15	4m54: determine, through investigation, the relationship between millilitres and litres
16 a)-b)	4m55: select and justify the most appropriate standard unit to measure mass (i.e., milligram, gram, kilogram) and the most appropriate standard unit to measure the capacity of a container (i.e., millilitre, litre)
17 a)-b)	4m56: solve problems involving the relationship between years and decades and between decades and centuries
18 a)–b)	4m57: compare, using a variety of tools (e.g., geoboard, pattern blocks, dot paper), two-dimensional shapes that have the same perimeter or the same area

Part C: Performance-Based Assessment

Administration

The two performance tasks in Part C are designed to provide insight into how well students are able to perform in terms of the categories of the Ontario Achievement Chart: Knowledge and Understanding, Thinking, Communication, and Application.

Since all of the specific and overall expectations for this strand have been assessed through the Concepts and Skills Assessment in Part B, it is recommended that you select one performance task for the Measurement Strand.

Read all parts of the problem orally to students. Tell students that they should provide detailed answers to the problem, including showing how they solved the problem. Remind students that they may use pictures, numbers, words, diagrams, and/or charts to explain effectively how they solved the problem.

Timing

Each task is designed to be completed in a 45- to 60-minute period. If necessary, provide additional time as long as students complete the task in one sitting.

Accommodating Students with Special Needs

If individual students have difficulties explaining their thinking in writing, consider providing scribes to record for the students or encourage students to show and explain their thinking using concrete materials.

Scoring the Assessment

A general rubric based on the Ontario Achievement Chart for Mathematics has been provided on page 115 to assist with scoring student responses to the tasks. Spend some time reviewing the anchors and rationales provided for each level of achievement on pages 116 to 131. The four categories should be considered as interrelated, reflecting the wholeness and interconnectedness of learning. Each student's performance should therefore be determined holistically by selecting the level that best describes the student's overall achievement.

Sometimes a student will not achieve at the same level for each criterion within a category or across categories. For example, a student may perform at Level 3 on Knowledge and Understanding, Thinking, and Application but at Level 2 on Communication. While you may determine that, overall, the student performed most consistently at Level 3, you may want to make a note that this student would benefit from additional instruction in the area of Communication.

Note: When scoring student work on the performance tasks, it is appropriate to note what you observed and heard while the student worked on the task.

Once you have completed scoring the students' assessments, you will need to record the results. You may record the results electronically using the ONAP 5 CD-ROM, or use a photocopy of the Performance Task Class Tracking Sheet provided on page 114.

Next Steps

Strategies for improving performance in the four areas of the Achievement Chart are provided in the ONAP introduction, pages 18 and 19.

Performance Task 1: Determining Dimensions

Materials

	FOR THE TEACHER		FOR EACH STUDENT		FOR EACH GROUP OF STUDENTS
•	Performance Task Class Tracking Sheet: p. 114 Performance Task Rubric: p. 115	•	BLM C1: Performance Task 1: Determining Dimensions: p. 111 grid paper	•	small counters (e.g., centicubes, snap cubes, bingo chips)
•	anchors and rationales: p. 116 ONAP 5 CD-ROM (optional)	• • •	colour tiles pencil eraser calculator		

Introducing the Task

In this task, students are asked to determine how to divide a ribbon into lengths to go around the perimeter of a bulletin board, and to calculate the possible dimensions and areas of the bulletin board.

Tell students that they will

- determine the possible dimensions of the bulletin board given the length of ribbon
- determine the possible areas of the bulletin board

Have students use BLM C1: *Performance Task 1: Determining Dimensions* to complete this activity.

Answers

- **1. a)** Four possible dimensions:
 - $8 m \times 1 m$ $7 m \times 2 m$ $6 m \times 3 m$ $5 m \times 4 m$
 - **b)** Sample answer: Perimeter is the distance around the bulletin board. There are 4 sides in total, but only 2 dimensions. I knew the longest and skinniest would be 8 m on two sides and 1 m on the other two sides. Then I made an organized list. The long side went down by 1 m each time. The next one would be 4 m \times 5 m, but that is really the same as 5 m \times 4 m, so I knew I had them all.
 - c) I would choose the 5 $m \times 4$ m bulletin board because it has the greatest area. It is 20 m^2 in area, which is more than all of the others.

 $5 \times 4 = 20 m^{2}$ $8 \times 1 = 8 m^{2}$ $7 \times 2 = 14 m^{2}$ $6 \times 3 = 18 m^{2}$ The more area that the bulletin board has, the more space there is for display.

Performance Task 2: Spilled Milk

Materials

	FOR THE TEACHER		FOR EACH STUDENT		FOR EACH GROUP OF STUDENTS
•	Performance Task Class Tracking Sheet: p. 114	•	BLM C2: Performance Task 2: Spilled Milk:	•	small counters (e.g., centicubes, snap cubes)
•	Performance Task Rubric: p. 115	•	p. 113 pencil		
•	anchors and rationales: p. 116	•	eraser calculator		
•	ONAP 5 CD-ROM (optional)				

Introducing the Task

In this task, students will determine how many different ways they can measure the amount of spilled milk and explain their reasoning.

Have students use BLM C2: Performance Task 2: Spilled Milk to complete this activity.

Answers

1. You could put a string around the edges of the puddle. Then you could measure how long the string is in centimetres, and that would tell you the perimeter of the puddle.

You could draw a rectangle that covers most of the puddle. You would measure the sides, and then multiply the width and length and get close to the area of the puddle. The area could be in square centimetres.

You could pour the puddle into a measuring cup. That would tell you how many millilitres of milk is spilled.

You could look at the container that the milk spilled from and figure out how much milk it could hold before the milk spilled. Then you could figure out how much milk it holds now that some has spilled. Then you could figure out how much milk spilled by subtracting these amounts.

You could pour the milk into a glass and then measure the combined mass of the glass and the milk. Then you could pour out the milk and measure the mass of the glass. Subtract the mass of the glass from the mass of the milk and glass together, and you will know the mass of the milk alone. The mass would be in grams. Name: Date:

Performance Task 1: Determining Dimensions (page 1)

Alyssa has a piece of blue ribbon that is 18 m in length. She wants to use the ribbon to make a border for a rectangular bulletin board. The length and the width of the bulletin board are whole numbers of metres.

1. **a)** If Alyssa uses all of the ribbon, what are all the possible whole number dimensions of the rectangular bulletin board? List them below.

b) How do you know you have found all the possible combinations?

Name:

Date:

Performance Task 1: Determining Dimensions (page 2)

c) If you want to use the bulletin board that has the greatest area for display, which dimensions will you choose?

Explain your reasoning.

Name: _____ Date: _____

Performance Task 2: Spilled Milk

1. A puddle of milk was found on a table in the lunchroom. How many different ways could you measure the spilled milk?

Explain your thinking.

ONAP PERFORMANCE TASK CLASS TRACKING SHEET GRADE 5: MEASUREMENT PART C

Date: _____ Grade: _____

School: Board:

Teacher Name: _____

Performance Task Title: _____

Student Name	Level 1–4	Comments

Performance Task Rubric

Assessment of Le	arning – What to Look For	in Student Work		
CATEGORY	I TEVEL 1	LEVEL 2	LEVEL 3	LEVEL 4
Knowledge and Understanding	 demonstrates a limited or inaccurate understanding of the concepts needed to solve the problem demonstrates a limited or inaccurate knowledge of the specific concepts, terms, or procedural skills that have been taught 	 demonstrates some understanding of the concepts needed to solve the problem demonstrates some knowledge of the specific concepts, terms, or procedural skills that have been taught 	 demonstrates considerable understanding of the concepts needed to solve the problem demonstrates considerable knowledge of the specific concepts, terms, or procedural skills that have been taught 	 demonstrates a thorough understanding of the concepts needed to solve the problem demonstrates a thorough knowledge of the specific concepts, terms, or procedural skills that have been taught
Thinking	 demonstrates a limited understanding of the problem shows little or no evidence of a plan uses a strategy and attempts to solve the problem but does not arrive at an answer 	 demonstrates some understanding of the problem shows some evidence of a plan carries out the plan to some extent by using a strategy and develops a partial and/or incorrect solution 	 demonstrates considerable understanding of the problem shows evidence of an appropriate plan carries out the plan effectively by using an appropriate strategy and solving the problem 	 demonstrates a thorough understanding of the problem shows evidence of a thorough plan shows flexibility and insight when carrying out the plan by trying and adapting when necessary one or more strategies to solve the problem
Communication	 provides a limited or inaccurate explanation/ justification that lacks clarity or logical thought communicates with limited effectiveness (may include words, pictures, symbols, and/or numbers) 	 provides a partial explanation/justification that shows some clarity and logical thought communicates with some effectiveness (may include words, pictures, symbols, and/or numbers) 	 provides a complete, clear, and logical explanation/ justification communicates with considerable effectiveness (may include words, pictures, symbols, and/or numbers) 	 provides a thorough, clear, and insightful explanation/justification communicates with a high degree of effectiveness (may include words, pictures, symbols, and/or numbers)
Application	 demonstrates a limited ability to apply mathematical knowledge and skills 	 demonstrates some ability to apply mathematical knowledge and skills 	 demonstrates a considerable ability to apply mathematical knowledge and skills 	 demonstrates a sophisticated ability to apply mathematical knowledge and skills

Performance Task 1: Determining Dimensions LEVEL 1 (Anchor 1)

Knowledge and Understanding

- demonstrates a limited and inaccurate understanding of area and perimeter; does not know procedure for finding area
- identifies three of four rectangles correctly, but rationale indicates confusion as to whether perimeter is additive or multiplicative
 unit use is correct

Communication

- provides an explanation in 1 b) that is not logical
 - provides an explanation in 1 c) that lacks clarity



Thinking

- demonstrates a limited understanding of the problem
- applies a flawed strategy of multiplying like dimensions to determine area, but the actual multiplication is quite good

Application

 demonstrates a limited ability to apply knowledge of perimeter to solve a problem



Performance Task 1: Determining Dimensions LEVEL 1 (Anchor 2)

Knowledge and Understanding

• demonstrates a limited and inaccurate understanding of both perimeter and area

Communication

- provides both limited and inaccurate explanations
 - states numerical value but does not use any units

Thinking

- demonstrates a limited understanding of the problem by identifying several rectangles, one of which is correct
 - uses a strategy that results in an incorrect answer in 1 c) by selecting the rectangle that is longest

- demonstrates a limited ability to apply an understanding of perimeter to solve a problem
- demonstrates some understanding of perimeter but not area





Performance Task 1: Determining Dimensions LEVEL 2 (Anchor 1)

Knowledge and Understanding

 demonstrates some understanding of the concept of perimeter but no understanding of area

Communication

- provides an explanation in 1 b) that is somewhat logical but lacks
 - clarity

Thinking

- identifies all of the perimeter possibilities correctly and shows some evidence of a plan
 - develops an incorrect solution for the question related to area

Application

demonstrates some ability to apply knowledge of perimeter to solve a problem



Performance Task: Determining Length (page 2)

c) If you want to use the bulletin board that has the greatest area for display, which dimensions will you choose? Explain your reasoning.

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Performance Task 1: Determining Dimensions LEVEL 2 (Anchor 2)

Knowledge and Understanding

- articulates some understanding of area and perimeter (correctly identifies two possible rectangles given a specific perimeter but is not able to identify the area)
- demonstrates some knowledge of specific concepts and correctly identifies units used to measure perimeter and area

Communication

 provides a partial explanation using both numbers and words with some effectiveness



Thinking

indicates some understanding of the problem (develops a partial solution related to perimeter)

- employs some ability to apply understanding of perimeter to solve the problem incompletely
- demonstrates confusion about the procedure used to determine area, which leads to an incorrect response, although the largest area of these two samples was selected in 1 c)



Performance Task 1: Determining Dimensions LEVEL 3 (Anchor 1)

Knowledge and Understanding

- demonstrates considerable understanding of procedures for
- determining the perimeter and area of rectanglesunderstands that perimeter is additive and area is multiplicative

Communication

- provides a logical explanation
- communicates effectively using mathematical language and diagrams

Thinking

articulates considerable understanding of the problem
 selects an appropriate strategy—organized list

· outers all appropriate straight

- indicates considerable ability to apply knowledge of perimeter and area to solve a problem
- sees beyond procedures and is able to articulate a relationship between area and perimeter





Performance Task 1: Determining Dimensions LEVEL 3 (Anchor 2)

Knowledge and Understanding

• demonstrates considerable understanding of perimeter and area

Communication

- provides a complete explanation
- provides justifications that could be more clearly articulated; there is evidence of confusion about procedures for determining perimeter and area in the explanation of 1 b)

Performance Task: Determining Length (page 1)Alyses the a place of blue ribbon, that is 18 m in length. She wants to use the ribbon to make a worder for a rectangular bulletin board? Last them blow, what are all the possible dimensions of the rectangular bulletin board? Last them blow.Distribution of the ribbon, what are all the possible dimensions of the rectangular bulletin board? Last them blow.Distribution of the ribbon, what are all the possible dimensions of the rectangular bulletin board? Last them blow.Distribution of the ribbon, what are all the possible dimensions of the rectangular bulletin board? Last them blow.Distribution of the ribbon, what are all the possible dimensions of the rectangular bulletin board? Last them blow.Distribution of the ribbon, what are all the possible dimensions of the rectangular blow.Distribution of the ribbon, what are all the possible dimensions of the rectangular place, it could be 2 m unde a 2 m long and 2 m long.Distribution of the ribbon to make a place of the ribbon to make a place of the ribbon to make a place of the ribbon of the ribbon to ribbon.Distribution of the ribbon to make a place of the ribbon to ribbo

Thinking

- indicates considerable understanding of the problem
- shows evidence of an appropriate plan for determining all of the possible dimensions as the answer is correct; however, the reasoning is flawed

- demonstrates considerable ability to apply knowledge of perimeter and area to solve a problem
- applies understanding of procedures to identify a relationship between area and perimeter

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Performance Task 1: Determining Dimensions LEVEL 4 (Anchor 1)

Knowledge and Understanding

demonstrates a thorough understanding of perimeter and area

Communication

- provides a thorough and clear explanation
- supplies effective explanations that are supported by clear and labelled diagrams •



Thinking

 demonstrates the ability to think with flexibility about the problem applies a plan that is thorough and incorporates several strategies

Application

- displays a sophisticated ability to apply understanding of area and perimeter to solve a problem
- applies an understanding of congruence to justify premise that all possible dimension combinations had been identified •

Performance Task: Determining Length (page 2)

c) If you want to use the bulletin bound that has the greatest area for display, which dimensions will you choose? Explain your reasoning.

dfoorst by width on each shape, because, length times each shape and 144 had the greatest area. width sives up the area of the shape and after I did that I laaked at the area of combinations I drew 5x4 had the biggest I would use. 5X4 because out of all the know this because I timesed Oreo.

Performance Task 1: Determining Dimensions LEVEL 4 (Anchor 2)

Knowledge and Understanding

- demonstrates a thorough understanding of perimeter and area
- articulates a clear understanding of the concept of maximizing area with respect to perimeter

Communication

communicates with a high degree of effectiveness using multiple representations

Thinking

- demonstrates a thorough understanding of the problem
- uses an appropriate strategy for ensuring that all length and width combinations are identified

Application

 provides a clearly articulated rationale for area dimensions based on a sophisticated understanding of maximizing area





Performance Task 2: Spilled Milk LEVEL 1 (Anchor 1)

Knowledge and Understanding

- demonstrates a very limited and inaccurate understanding of measurement concepts
- supplies numbers on the diagram that indicate some understanding of relative size

Communication

• provides a limited and largely irrelevant explanation

Thinking

- demonstrates a limited understanding of the problem by attempting to list different ways spilled milk could be measured
 - uses a strategy that does not connect measurable attributes or units to the problem

Application

 displays a limited ability to apply knowledge of measurement to solve the problem



Performance Task 2: Spilled Milk LEVEL 1 (Anchor 2)

Knowledge and Understanding

• demonstrates a limited understanding of measurement concepts

Communication

• provides explanations that are both limited and inaccurate

Thinking

- indicates a limited understanding of the problem as three different ways to measure the milk are listed
 - shows little evidence of a plan

- demonstrates a limited ability to apply measurement concepts to solve a problem
 - indicates that a string could be used but does not connect measurement to perimeter, identifies that area could be measured but does not indicate how



Performance Task 2: Spilled Milk LEVEL 2 (Anchor 1)

Knowledge and Understanding

 demonstrates an understanding of some measurement concepts but lacks the ability to differentiate between measurable attributes and related units

Communication

- communicates with some effectiveness
 - provides a list that lacks organization

Thinking indicator

- indicates some understanding of the problem in that there is a definite attempt to list many ways
 - identifies a strategy that leads to a list that is somewhat elaborate but also imprecise and random

- demonstrates some ability to apply mathematical knowledge of measurement attributes and units
 - provides a response that reflects some confusion between measurement attributes and units

Derimetera 58 30 g or kg. 60 68 taking a Sacczing The jun 6 inches Km area www and 8 a) How many different ways could you measure the spilled milk? Explain your thinking. Performance Task: Spilled Milk cup-in and 2 2 A puddle of milk was found on a table in the lunch roor 2 medsuge meduren MACASMER medense measure measurang heigh measure measure Sucing it medsure measure you could and cout d could 8 COUL coul coul coul COUL COUL atin vou 104 non DU 104 10 M OUL 10U 104 5

Performance Task 2: Spilled Milk LEVEL 2 (Anchor 2)

Knowledge and Understanding

• demonstrates an understanding of some measurement concepts

Communication

- provides a partial explanation
- offers an explanation related to determining capacity that is confusing and inexact

Thinking

- indicates some understanding of the problem
- develops a partial solution that is partially inaccurate

Application

applies some understanding of only two measurable attributes

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Performance Task 2: Spilled Milk LEVEL 3 (Anchor 1)

Knowledge and Understanding

- demonstrates considerable understanding of measurement concepts
- indicates an understanding of attributes that are measurable with some confusion between capacity and volume

Communication

• provides a clear explanation but communication would have benefited from the inclusion of appropriate units

Thinking

• articulates considerable understanding of the problem by identifying many measurable attributes

Application

• demonstrates considerable ability to apply general understanding of measurement with flexibility

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on a table in the lunch room.	could you measure the spilled	eperimiter becaute schape of the puddth e undth from on e width from on re the milk in capo vpan put it inami e notaure by puttin e votaure by puttin
. A puddle of milk was found	 a) How many different ways Explain your thinking. 	You could require the string, cut if to the four could measured to could measure to the oth er. You could measure to the oth er. You could measure low could measure to vould measure in the

Performance Task 2: Spilled Milk LEVEL 3 (Anchor 2)

Knowledge and Understanding

- demonstrates considerable understanding of measurement concepts
- indicates an understanding of measurable attributes but does not link these to units

Communication

• provides a logical explanation but communication would have benefited from the inclusion of appropriate units

Thinking

• demonstrates considerable understanding of the problem by identifying multiple and appropriate measurable attributes

Application

shows considerable ability to apply knowledge of measurement to solve a problem

String. You can abn 6 and then see how along the perimeter and is. You could also Usila 9 rule 10 measure with vou could count. the milk in a Will F a) How many different ways could you measure the spilled milk? Explain your thinking. Performance Task: Spilled Milk and 0 Ver A puddle of milk was found on a table in the lunch roon 20 area Ould z togetter heet cnp tho Measure Morak here String You could Square peicer mearuing measuring Fina/ nuch then even and tho the 0

Performance Task 2: Spilled Milk LEVEL 4 (Anchor 1)

Knowledge and Understanding

- demonstrates a thorough understanding of measurement concepts needed to solve the problem
- indicates a thorough knowledge of specific measurement concepts; includes an interesting distinction between mass and weight, but while there is evidence of understanding of both volume and capacity, the use of volume in this context is not appropriate

Communication

provides a clear and comprehensive explanation

You could measure the length by plicce of string agenst the side. You could measure the width the capacity putting the milt in a scale on bue side and put grams on the other side. You could measure the mass by You could measure the height could measure the weight or putting it on a scale and You could measure the volume by putting cabes in the milt. by a picce of string the perimeter or You covid put the MILK IN Performance Task: Spilled Milk a) How many different ways could you measure the spilled milk? Explain your thinking. -easing the numbers. A puddle of milk was found on a table in the lunch roor a Jar and measure by analar.

Thinking

demonstrates a thorough understanding of the problem

Application

• adapts measurement knowledge to solve the problem effectively

by putting a rular through the milk. You could measure the area by putting different shapes in the milk that are the same size.

Performance Task 2: Spilled Milk LEVEL 4 (Anchor 2)

Knowledge and Understanding

- demonstrates a clear understanding of measurement concepts
- connects measurement methods to appropriate attributes with accuracy

Communication

- provides a clear and organized explanation
- includes some units that provide specific attribute detail

Thinking

• demonstrates an accurate understanding of the problem

Application

applies understanding of measurement concepts to identify a good range of responses

deev cm on could measure the perimeter the milk. & measureing because you could get a transpar ent togethe Inon wany king the mill string a round the NO You could measure the area Performance Task: Spilled Milk a) How many different ways could you measure the spilled milk? Explain your thinking. the meagure how because un japos A puddle of milk was found on a table in the lunch roon toach megsare NON COULD Put it Into 6 meas they o'nd Stick.a 047 0 CON ON CONID IW because Sticing then MIK the cup. Pho Уои ML

Next Steps for Measurement

Instructional Next Steps for Overall Expectations

After summarizing individual and class performance on each overall expectation, you may find that there are areas that could be retaught to some students. The following suggestions have been provided to assist you in preparing tasks for individuals or small groups of students.

Overall Expectation 4m38 (Attributes, Units, and Measurement Sense) Estimate, measure, and record length, perimeter, area, mass, capacity, volume, and elapsed time, using a variety of strategies.

Background

This overall expectation is about strategies for estimating, measuring, and recording measurements. Inherent in this expectation are several foundational understandings in measurement. Students need to learn the attributes that they will measure; understand the structure and use of systems of measurement; select appropriate units and tools to measure to the degree of accuracy required in a particular situation; understand how to measure; and, more importantly, what it means to measure.

For further explanation, please see Baroody, Arthur. *Fostering Children's Mathematical Power: An Investigative Approach to K–8 Mathematics Instruction*. Mahwah, New Jersey: Lawrence Erlbaum Associates, 1998. pp. 15-4–15-5.

Strategies

The Concept of Measuring

Students need to understand what measurement is. Objects have many characteristics (attributes) that can be measured. When asked to measure, students must first decide what attribute needs to be measured. Does the object need to be matched to a unit of length, covered with a unit of area, or filled using a unit of capacity? Students learn to estimate by becoming familiar with benchmark measurements.

Students begin to understand the attributes of objects that can be measured (length, mass, capacity, etc.) by working with non-standard units. By the end of Grade 4, students will be familiar with standard metric units of length, mass, and capacity. They will have used non-standard units of volume. Students need many measurement opportunities to understand that the perimeter of a field is linear and therefore measured in units such as metres, which have the attribute of length. The area of the same field is measured in units such as square metres, which have the attribute of area.

Measuring Length

Students need to be able to measure length using standard metric measurement tools. It is important that they understand that it is the spaces between the marks on the measurement device that are being compared and counted. Activities such as the one following will help to reinforce this concept. Accurate measurement requires that students become skilled at using measurement instruments. Skills are developed through experience and practice.

How long is this line?



Give students many opportunities to measure. Have them measure a length in more than one unit (centimetres and millimetres). Have students measure length using combined units (1 metre 35 cm). Use manipulatives such as tiles and geoboards when investigating area. When measuring the areas of rectangles, relate multiplication arrays to grids so that students connect a 5×7 grid with a 5×7 array and 5 rows of 7 tiles with a rectangle measuring 5×7 .

Measuring Time

Measuring time and determining elapsed time can be challenging for students. There are 60 minutes in an hour, 24 hours in a day, 7 days in a week, etc. Relationships are no longer based on 10. Each unit of time has its own interval and unit of measurement. The numbers are no longer as friendly. Emphasize that with time, as with all measurement, a comparison is being made to a standard unit based on an attribute. Sixty minutes of time takes as long as one hour of time. The space between each number on a clock represents the length of five minutes.

When determining elapsed time, students are often confronted with two units of measure: hours and minutes. Allow students to develop and share strategies for determining elapsed time in a way that makes sense to them. Their calculation of elapsed time should rely on logic rather than an application of a procedure.

The skill of reading a clock or telling time is quite distinct from the measurement of time. Students need opportunities both to read and measure time.

Overall Expectation 4m39 (Measurement Relationships)

Determine the relationships among units and measurable attributes, including the area and perimeter of rectangles.

Background

This expectation is about the relationship between units in our base ten system of metric measurements as well as relationships between different attributes used to measure the same object, for example, area and perimeter.

Strategies

Metric Measurements

Provide students with many opportunities to measure lengths using metric measuring tools. Students need to "see" the 100 cm in a metre and the 10 mm in a cm. Use

benchmark lengths to help students estimate (a door is about 2 metres high, your small finger is about 1 cm in width).

Repetitive conversion questions do little to enhance measurement sense. Although the centimetre and metre are more commonly used than the decimetre as a measure of length, the difference in length between the two is significant and an intermediary reference point is beneficial.

Measuring Area and Perimeter

Relationships between linear units and area units and between area and perimeter can be very challenging for many students. Make the connection between attributes of the object and the unit used to measure the attribute explicit. Have students measure length with string and rulers (matching) and measure area with tiles (covering). Measure an object several ways. Measure the area of a desktop, measure the perimeter of a desktop, measure the height. Ask how could the mass of a desk be measured? Make connections between attributes, measuring devices, and units explicit. Give students many opportunities to investigate measurement.

Encourage students to explore the numerical patterns that underlie the formula for calculating perimeter and area. Students need to develop foundational understanding that will allow them to apply formulas with reason rather than rote memorization. Understanding is critical to avoid common student errors such as confusing the formulas for perimeter and area. By allowing students to investigate measurement relationships through a problem-solving approach prior to presenting formulas, the formulas are less likely to be forgotten, will be used flexibly, and are more likely to be expanded and adapted appropriately.

Measuring Time

Use number lines to help students visualize time. Students need to see the connection between linear measurement and the passage of time. Periods of time greater than a year have a base of 10 (10 years in a decade, 10 decades in a century, 100 years in a century). This base of 10 means students often grasp the relationships among years, decades, and centuries more quickly than the relationships among minutes, hours, days, and years.